

2-3 Coulomb corrections

4-5 Radiative corrections

6-Stability checks

7-9 Background level and shape systematics

10-Electron ID systematics

11-Trigger systematics

12-13 Resolutions

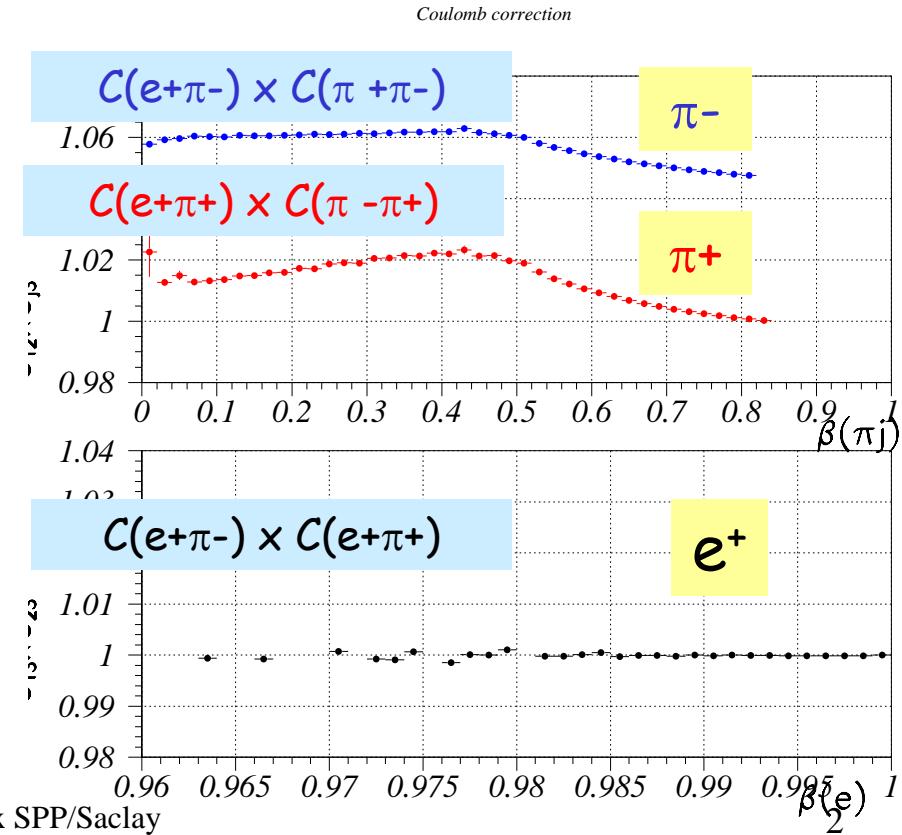
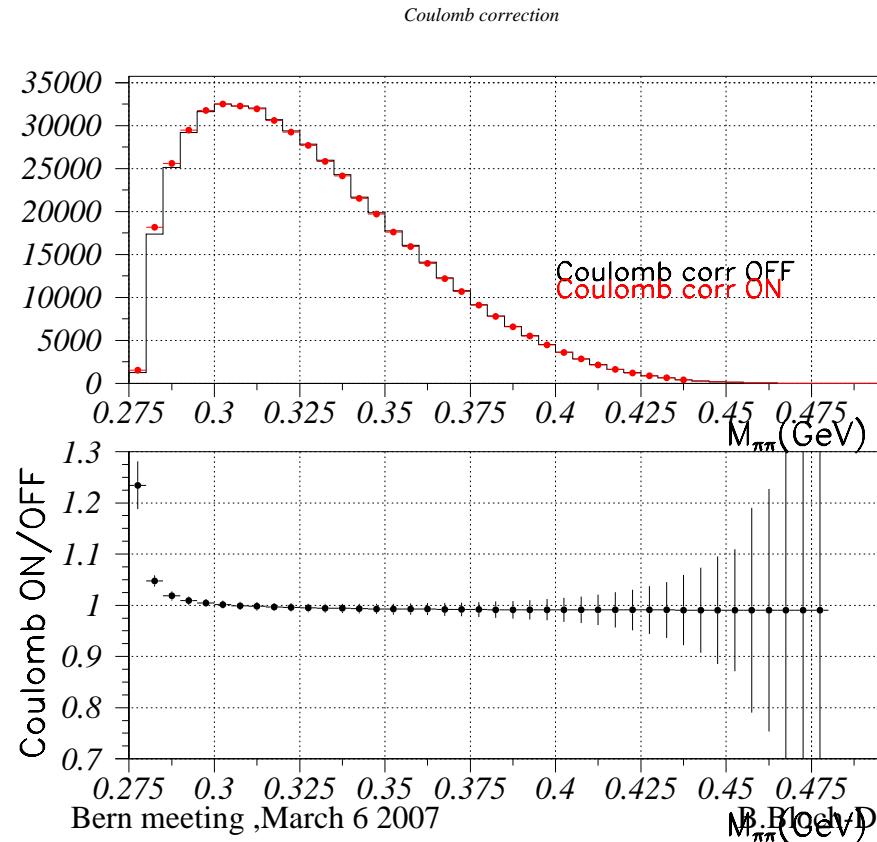
14-15 Acceptance

Classical Coulomb corrections

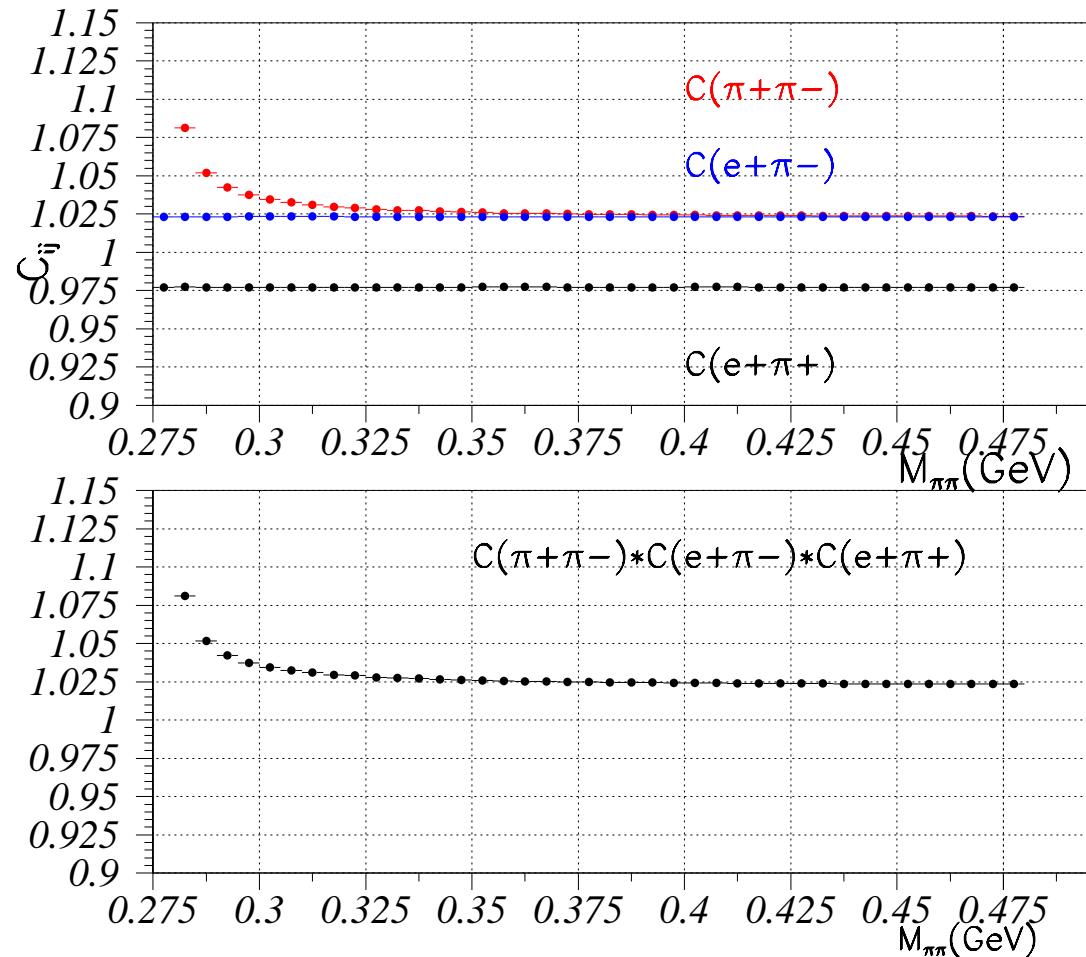
attraction/repulsion between opposite/same charge particles in the final state is implemented as a weight for each generated event : $C = C12*C13*C23$

Where $C_{ij} = n_{ij}/(e^{n_{ij}}-1)$ with $n_{ij} = 2\pi\alpha q_i q_j/v_{ij}$ and v_{ij} = relative velocity

The overall effect is a distortion of the $M_{\pi\pi}$ mass



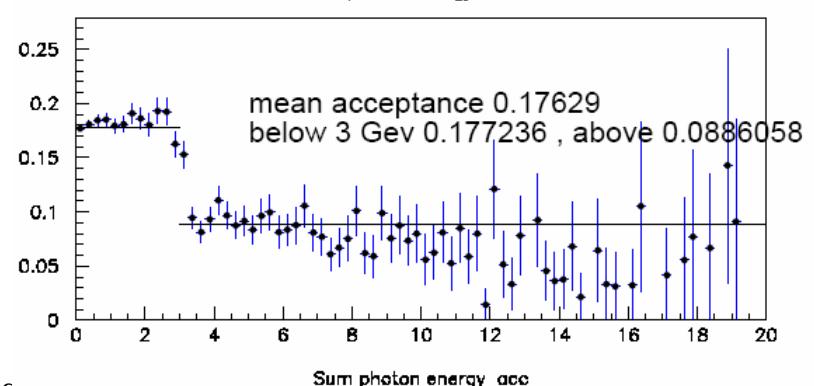
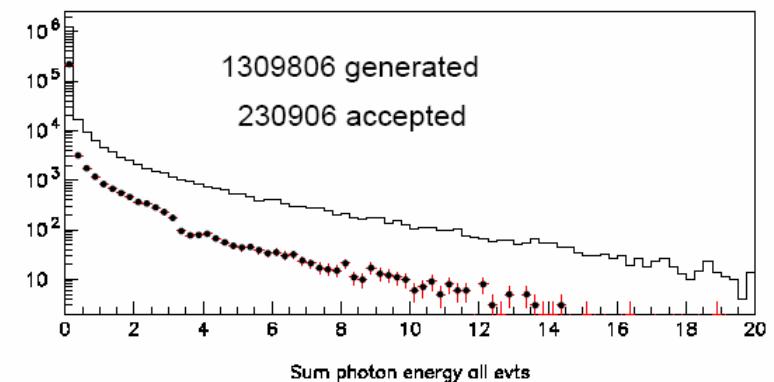
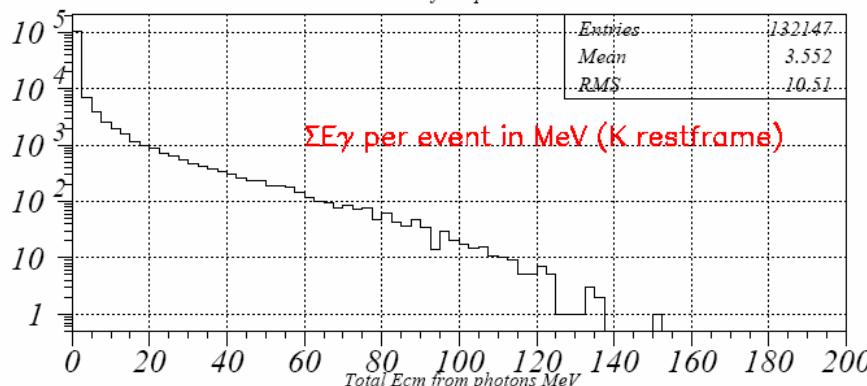
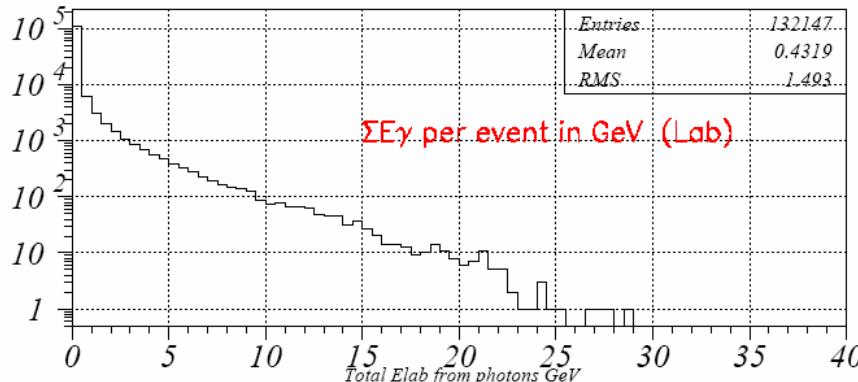
Coulomb correction

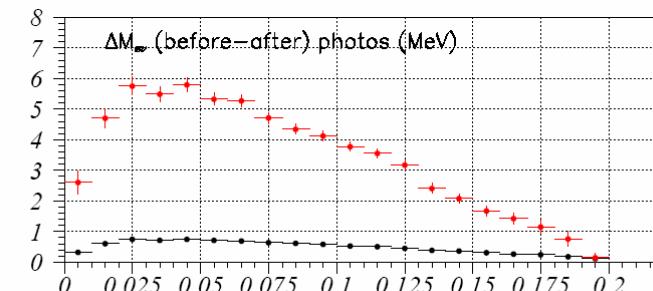
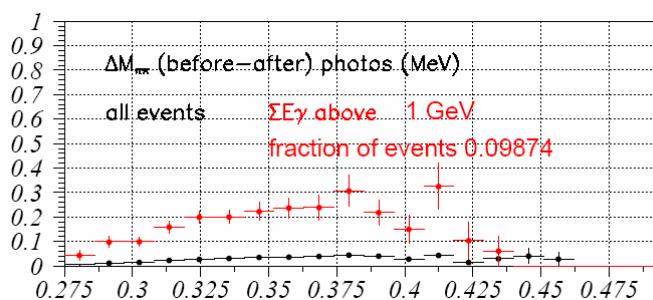
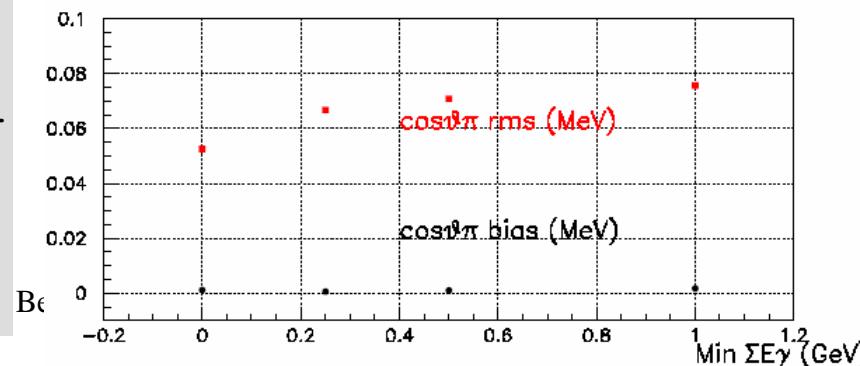
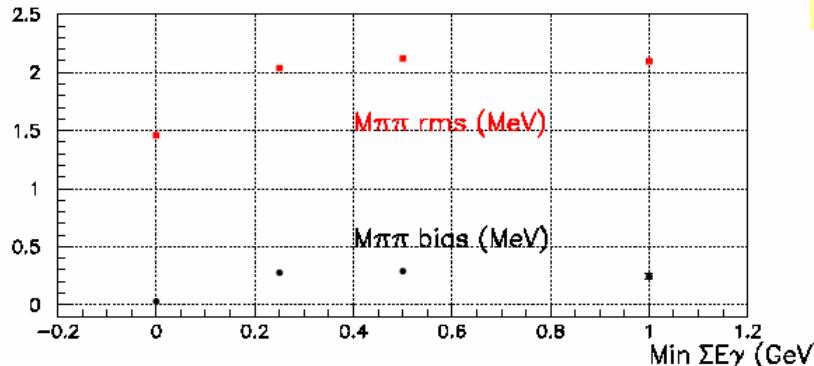
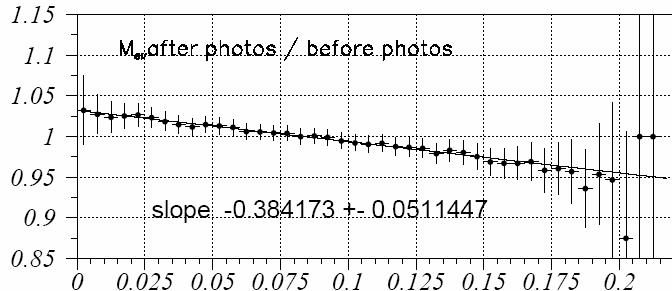
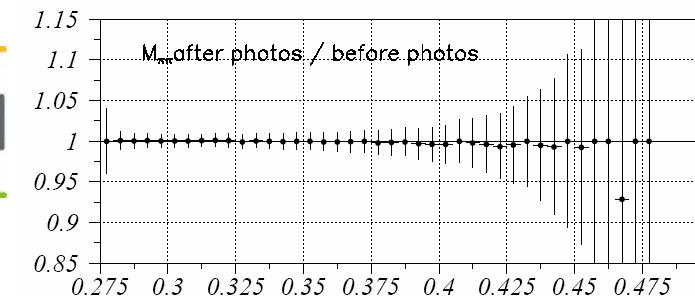


Simulation using PHOTOS version 2.15 from Z. Was et al.

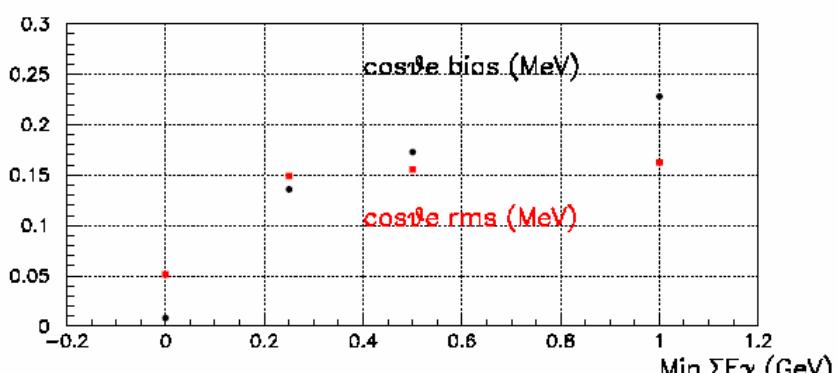
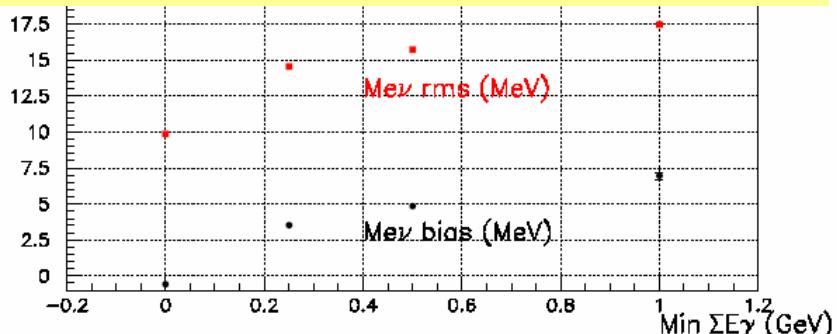
At high $M_{\pi\pi}$ mass, there is room for photon emission (and thus at low Mev mass)

~26% of events have "some" radiated photon energy (>0 GeV) but less than 10% have more than 1 GeV radiated. Above 3GeV radiated energy, the acceptance is even lower (cut at 3GeV non associated energy)

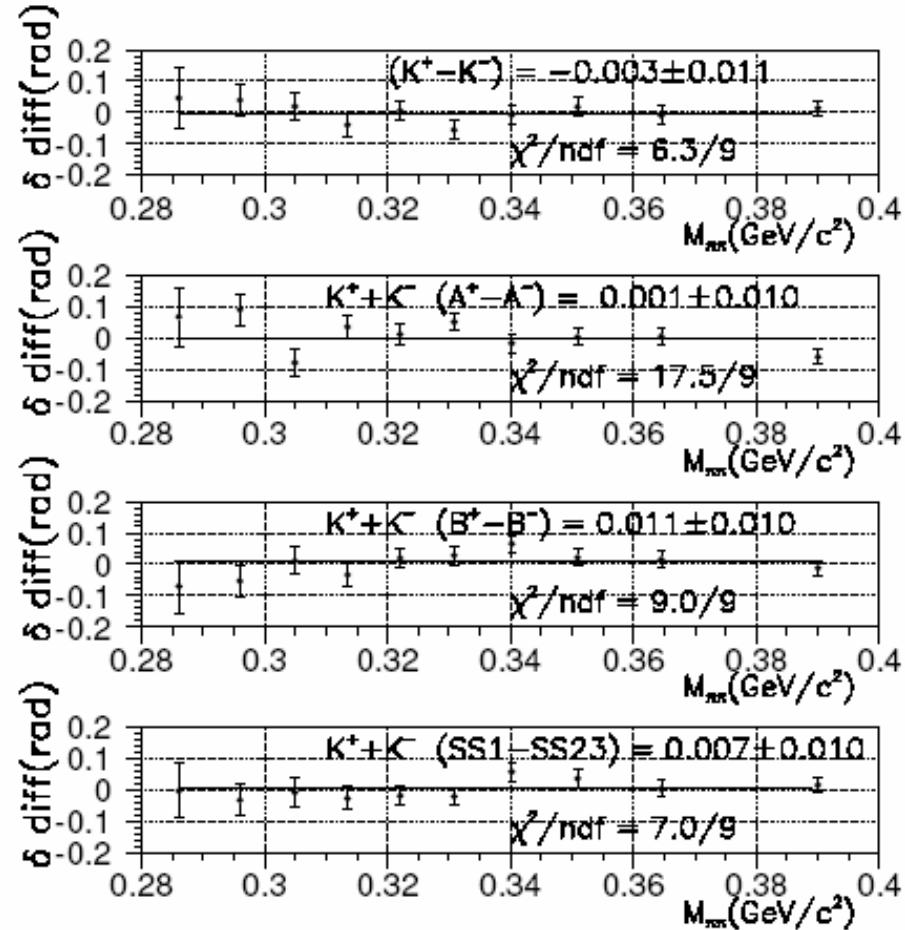
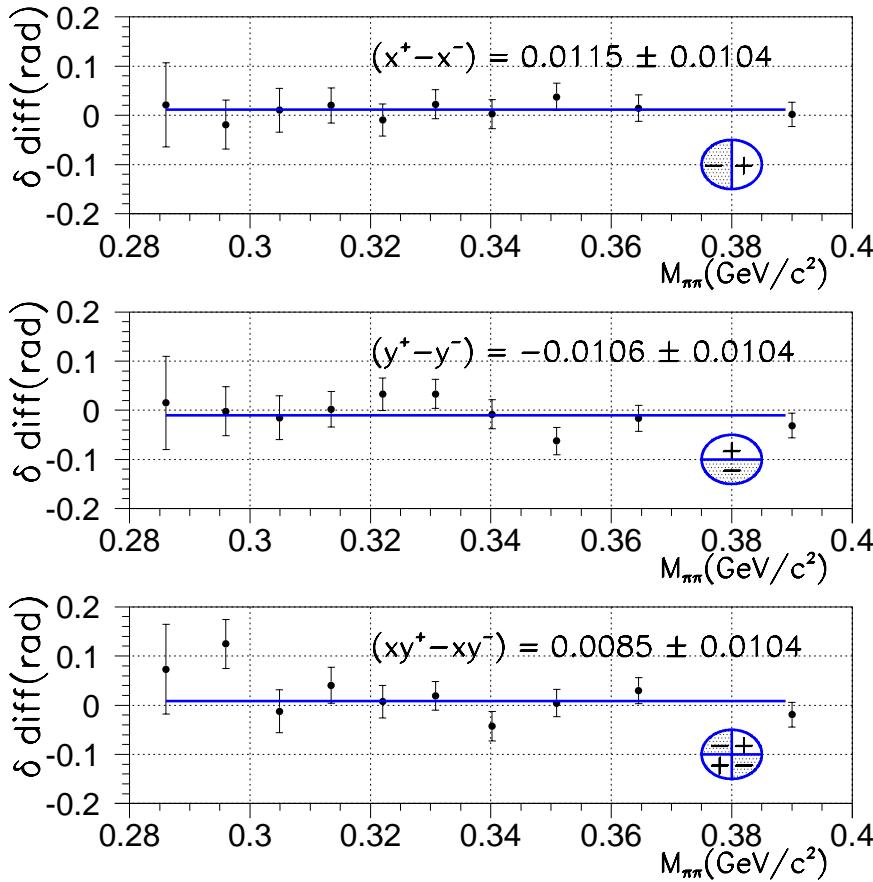




Largest effect on Mev and costheta variables



Electron impact in LKr calo, Kaon charge, Achromat and Magnet polarity, time ...



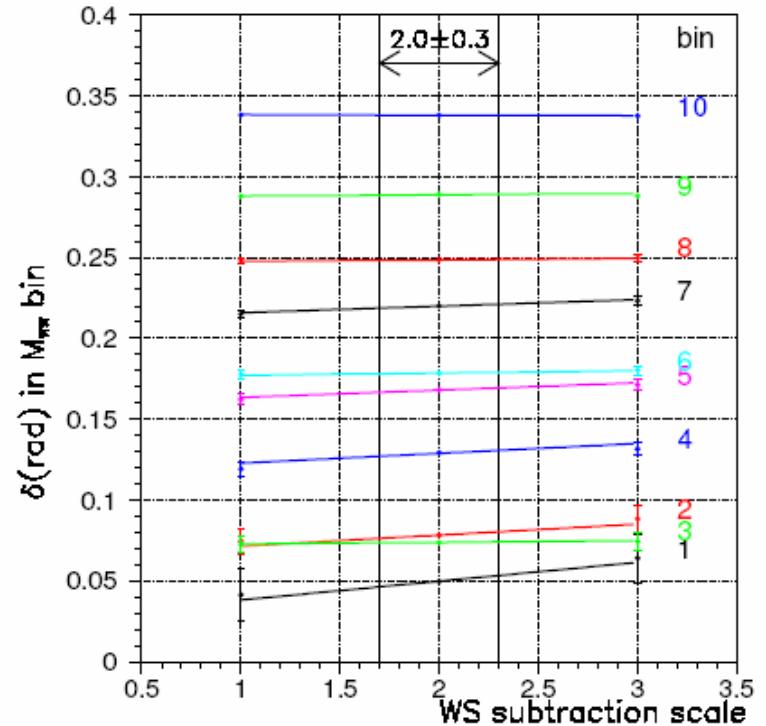
Background level control (1)

Method:

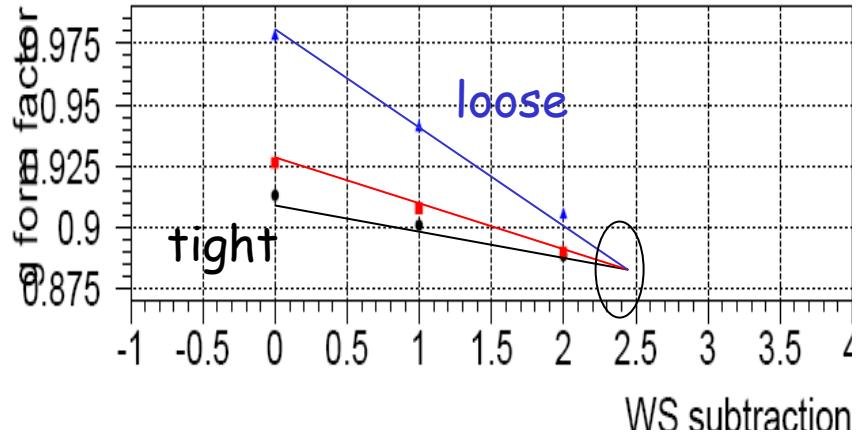
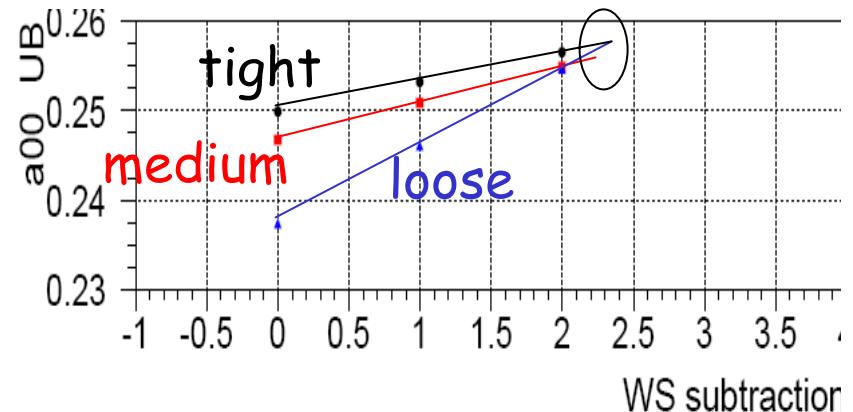
- subtract $1*WS, 2*WS, 3*WS$
- Measure slope $D\delta/Dbkg$ for each δ point

Quote $0.3*D\delta/Dbkg$ since we control the background subtraction as $(2. \pm 0.3)*WS$

Slopes are all positive, **bin to bin correlated**



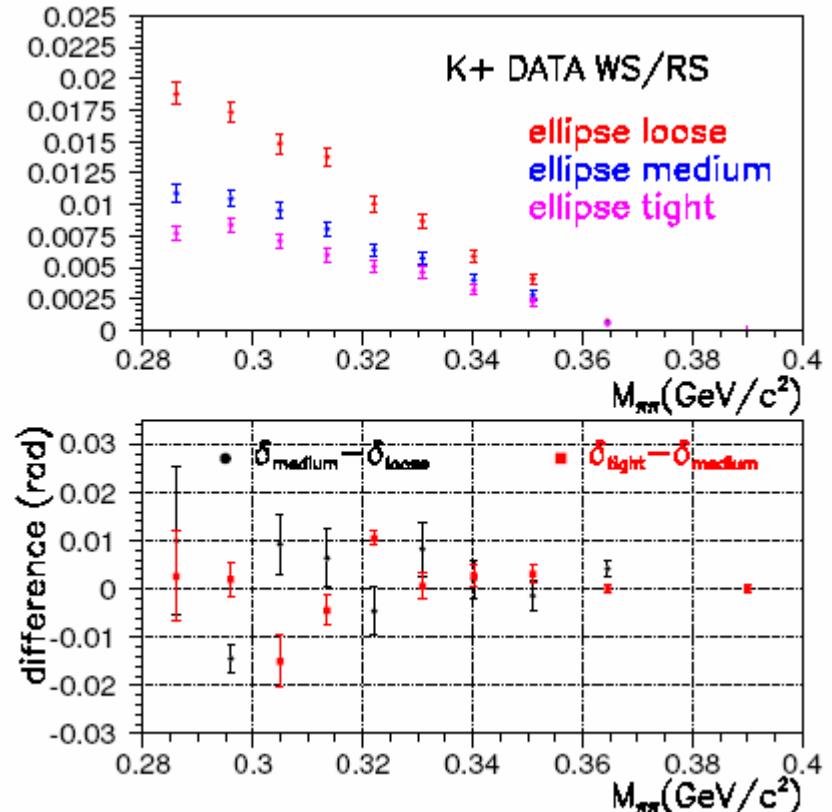
- Repeat for 3 ellipse cuts : the FF vary with the level of bkg subtracted but with different slopes
- The 3 lines **focus** to the same FF value when the **true level** is reached = $\sim 2.3 \times$ Wrong Sign events
- This factor 2.3 confirmed by summing all background processes contributing to signal with corresponding acceptance and branching fractions.



Method:

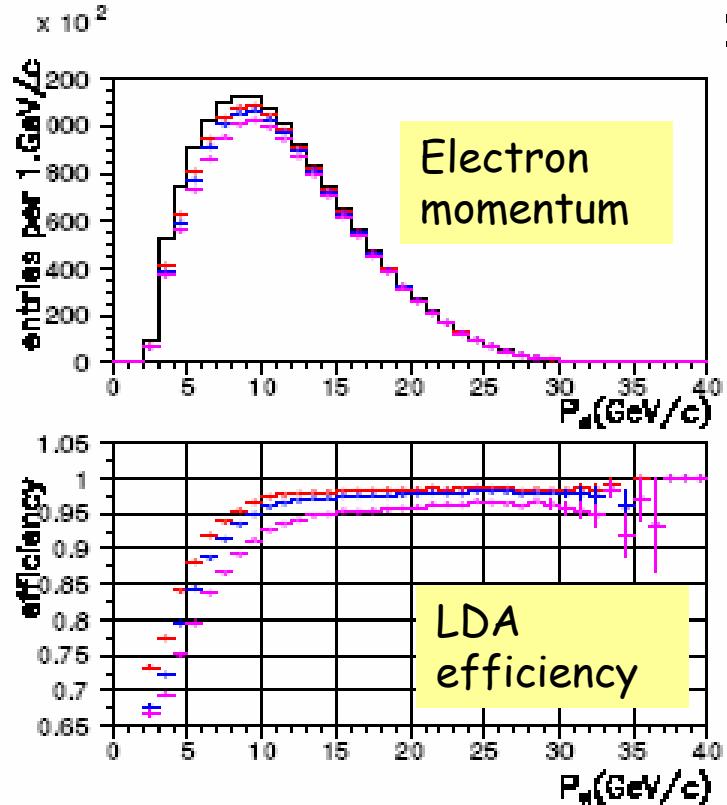
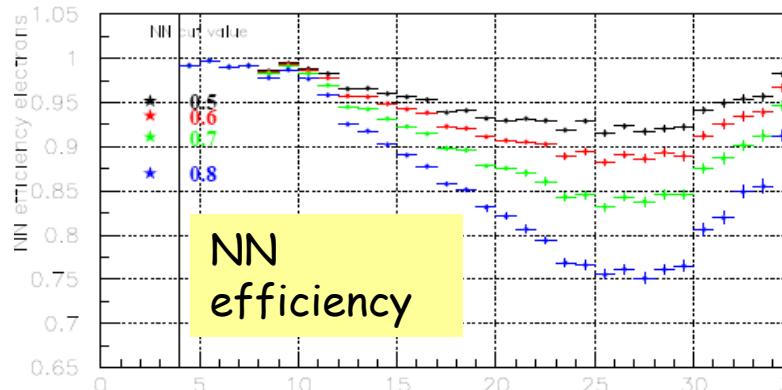
- Vary the ellipse cut in the plane $[M3\pi - MK, pt]$ from loose to medium to tight
- Background shape distorted (not scaled)
- Quote $0.5 * (D\delta_1 - D\delta_2)$ as variations are similar and remove both $\sim 2\%$ events

No bin to bin correlation



Method:

- Vary the LDA cut = (0.85, 0.90, 0.95) for Data and MC (applied to MC as a parametrized efficiency $f(P_{\ell})$),
- + compare NN (0.80) and LDA(0.90) results
- Quote weighted rms of the three numbers as variations are similar and bin to bin uncorrelated



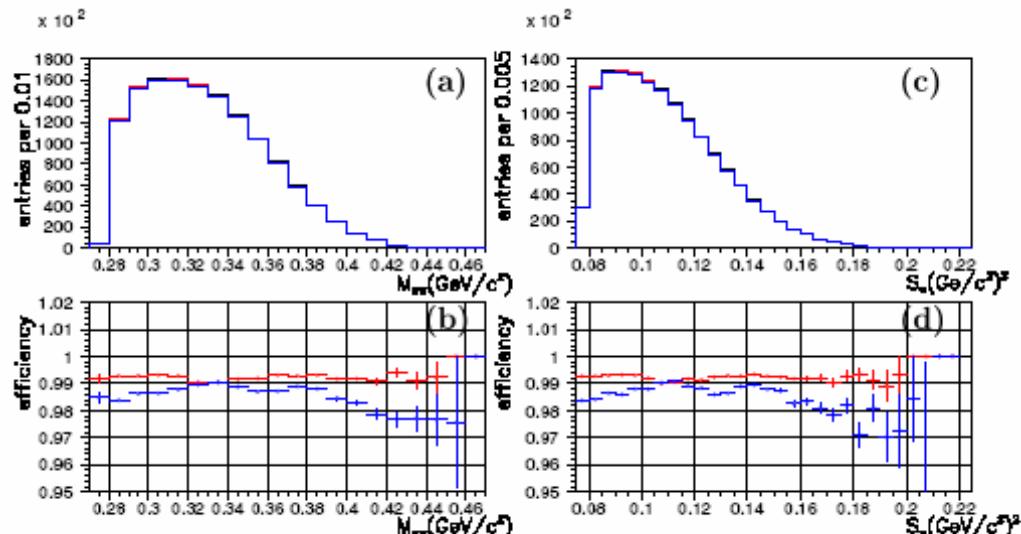
Trigger efficiency

2 Methods:

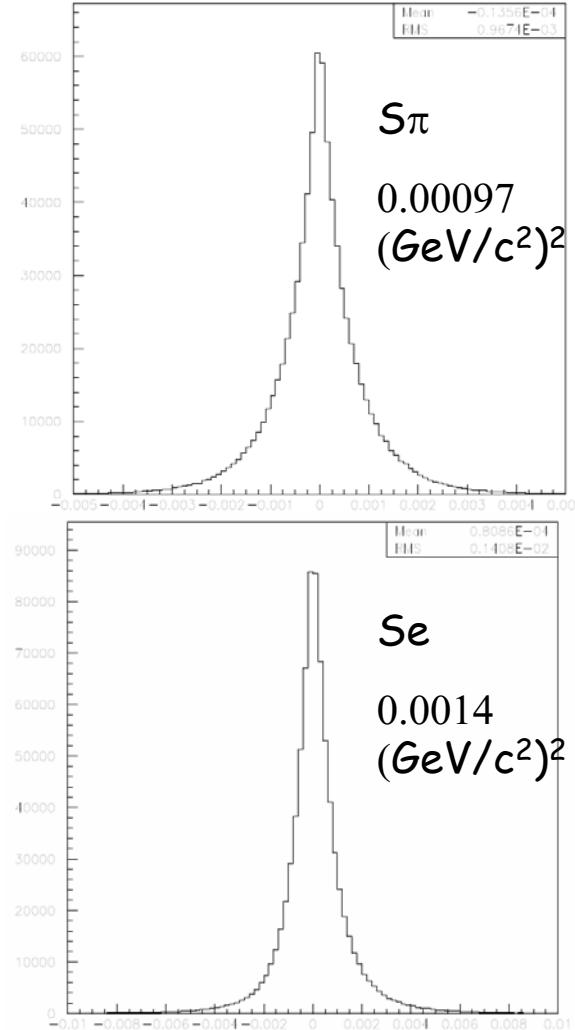
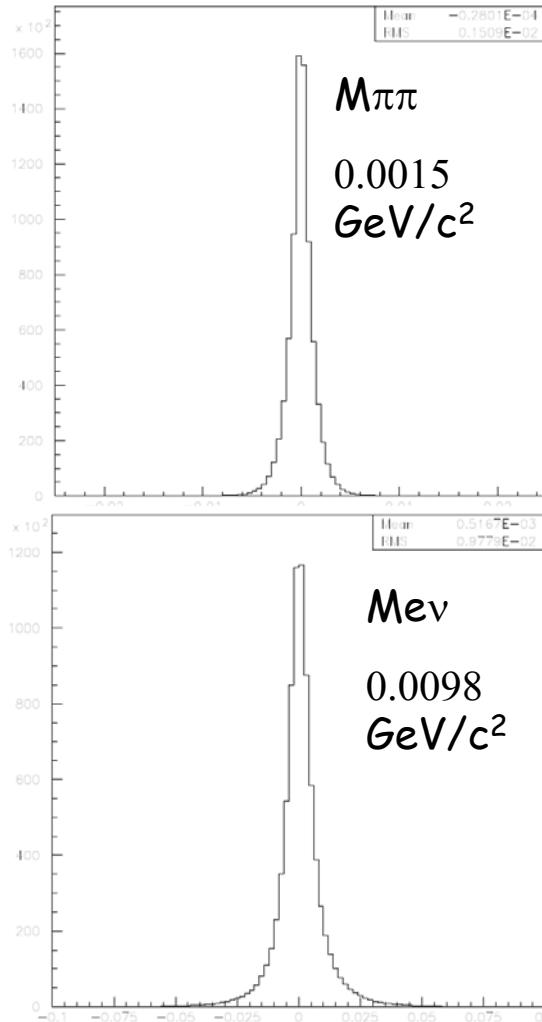
- evaluation from Minimum Bias triggers in 2003:
Efficiency = $(99.3 \pm 0.1)\%$, available as a matrix in the 5-dimension space of the C.M. variables.
- evaluation from $\pi\pi^0$ decays treated as Ke4 ($S\pi$ up to 0.225)
Efficiency = $(98.15 \pm 0.06)\%$, available as function of $S\pi$

Difference within 1% for significant acceptance regions

Effect on data is similar when efficiency applied to MC, \rightarrow average values, bin to bin uncorrelated



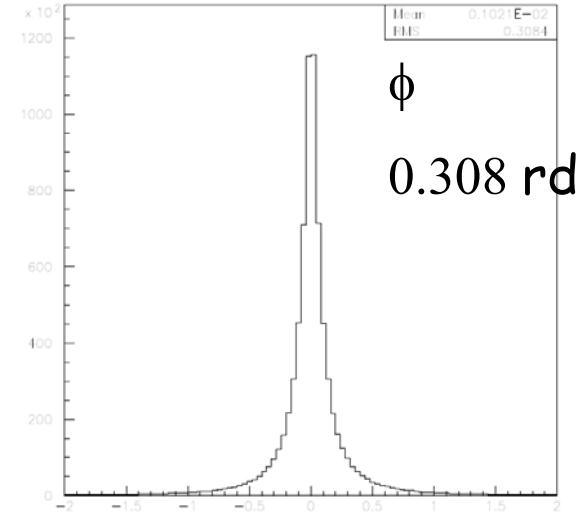
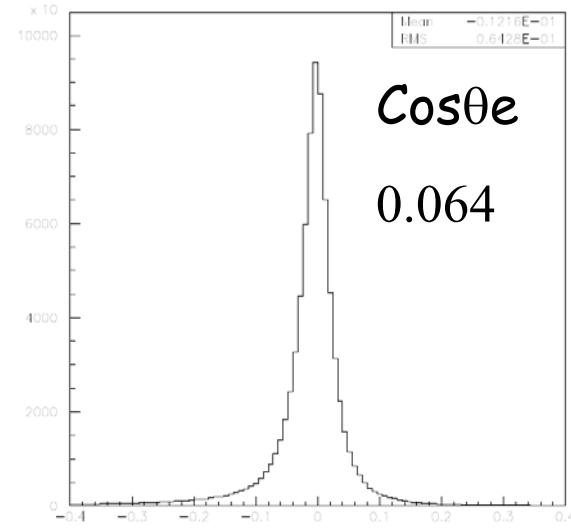
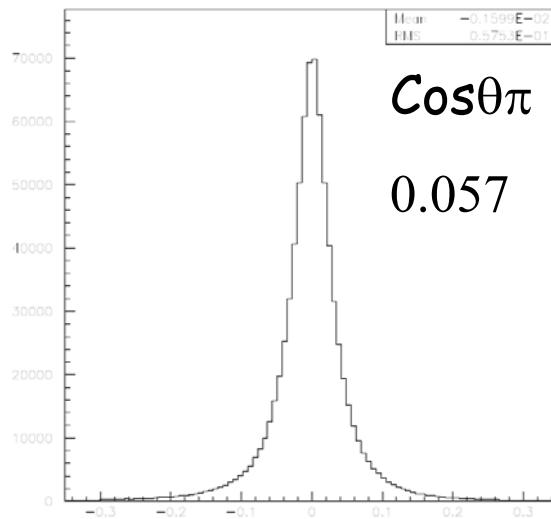
Resolution for C.M. variables : masses



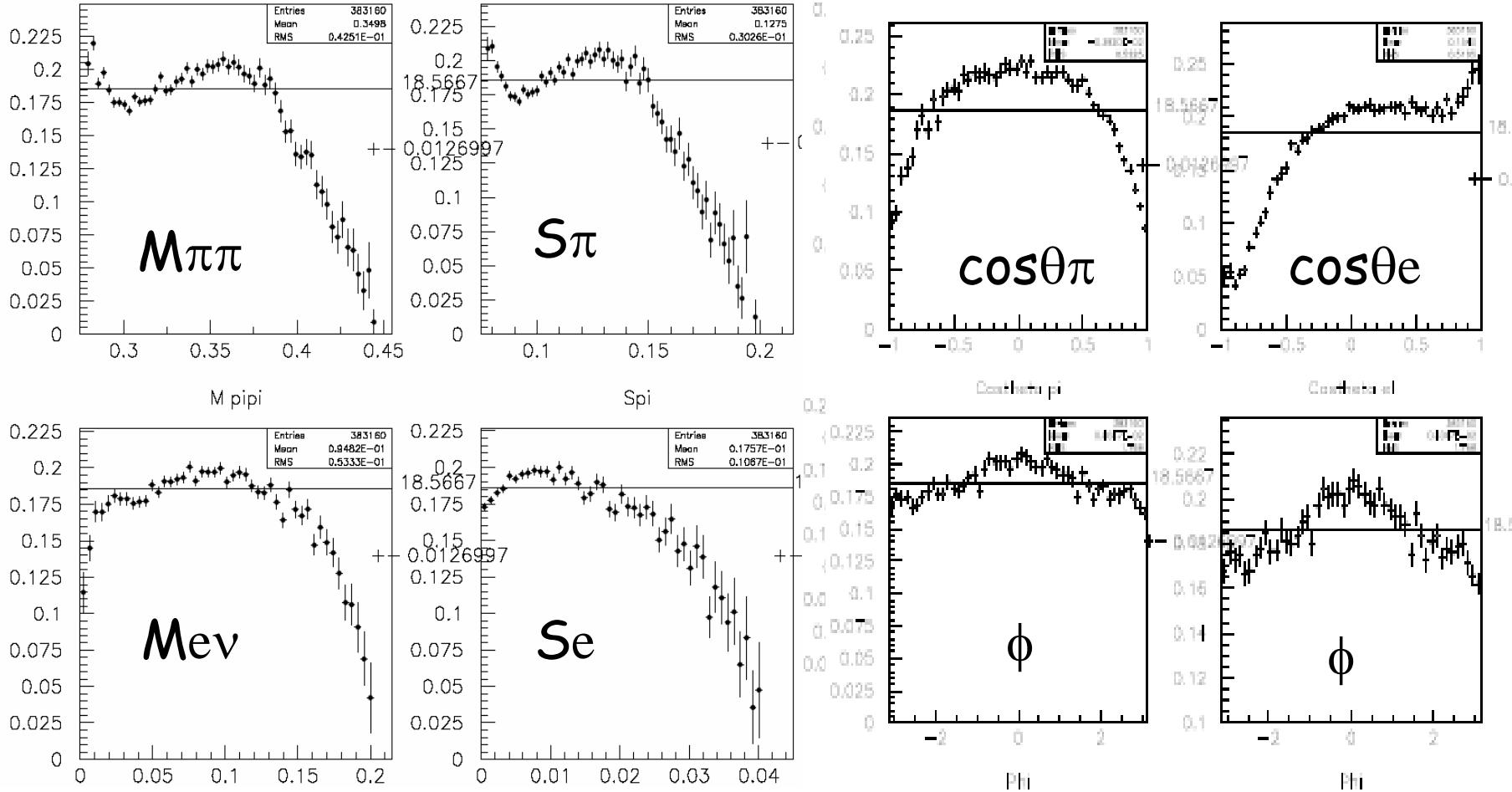
BNL for comparison :

 S_π $0.00133 \text{ (GeV}/c^2)^2$ S_e $0.00361 \text{ (GeV}/c^2)^2$ θ_π 0.147 (rad) θ_e 0.111 (rad) ϕ 0.404 (rad)

Resolution for C.M. variables : rms (angles)



Typically $18.57 \pm 0.01 \%$



The "Dalitz" plot ($M_{\pi\pi}$,Mev) bins