

- 2-3 Coulomb corrections
- 4-5 Radiative corrections
- 6-Stability checks
- 7-9 Background level and shape systematics
- 10-Electron ID systematics
- 11-Trigger systematics
- 12-13 Resolutions
- 14-15 Acceptance

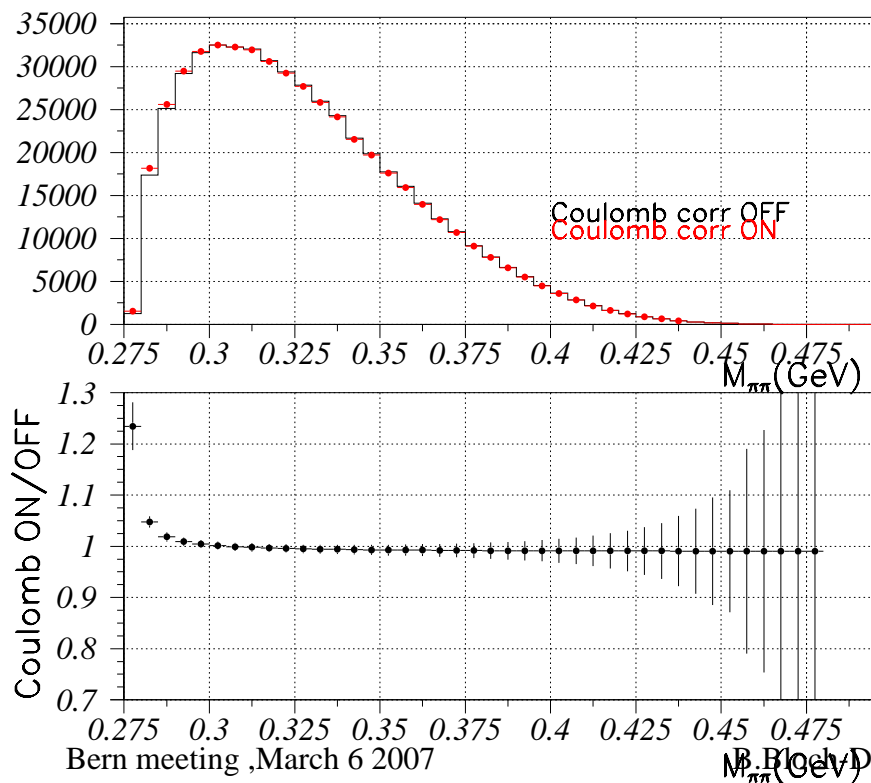
# Classical Coulomb corrections

attraction/repulsion between opposite/same charge particles in the final state is implemented as a weight for each generated event :  $C = C_{12} \times C_{13} \times C_{23}$

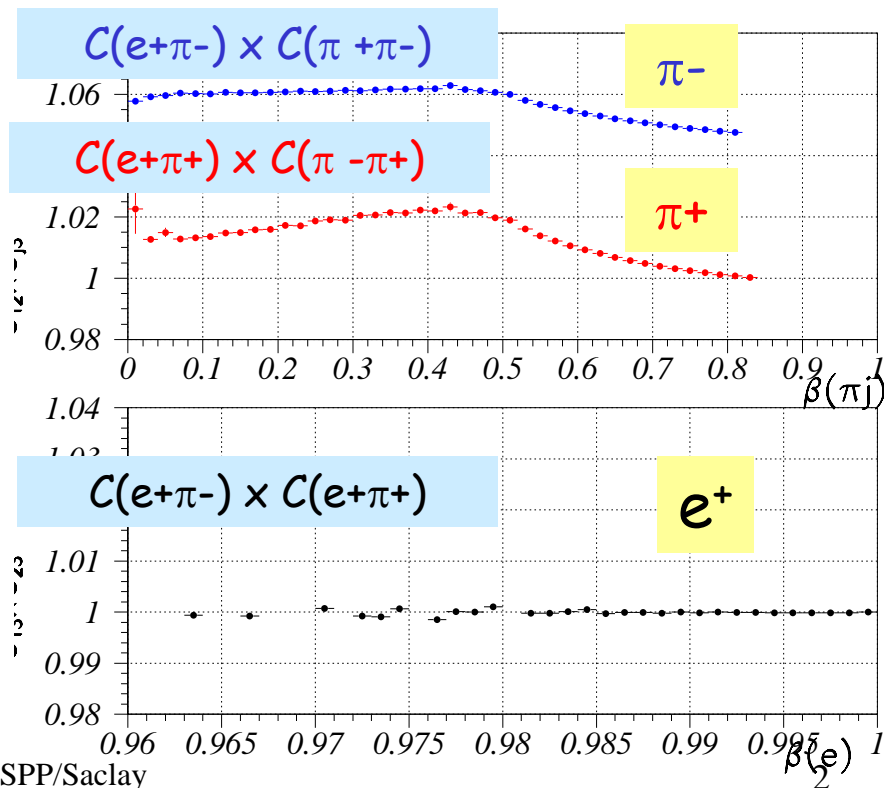
Where  $C_{ij} = n_{ij}/(e^{n_{ij}} - 1)$  with  $n_{ij} = 2\pi\alpha q_i q_j / v_{ij}$  and  $v_{ij}$  = relative velocity

The overall effect is a distortion of the  $M_{\pi\pi}$  mass

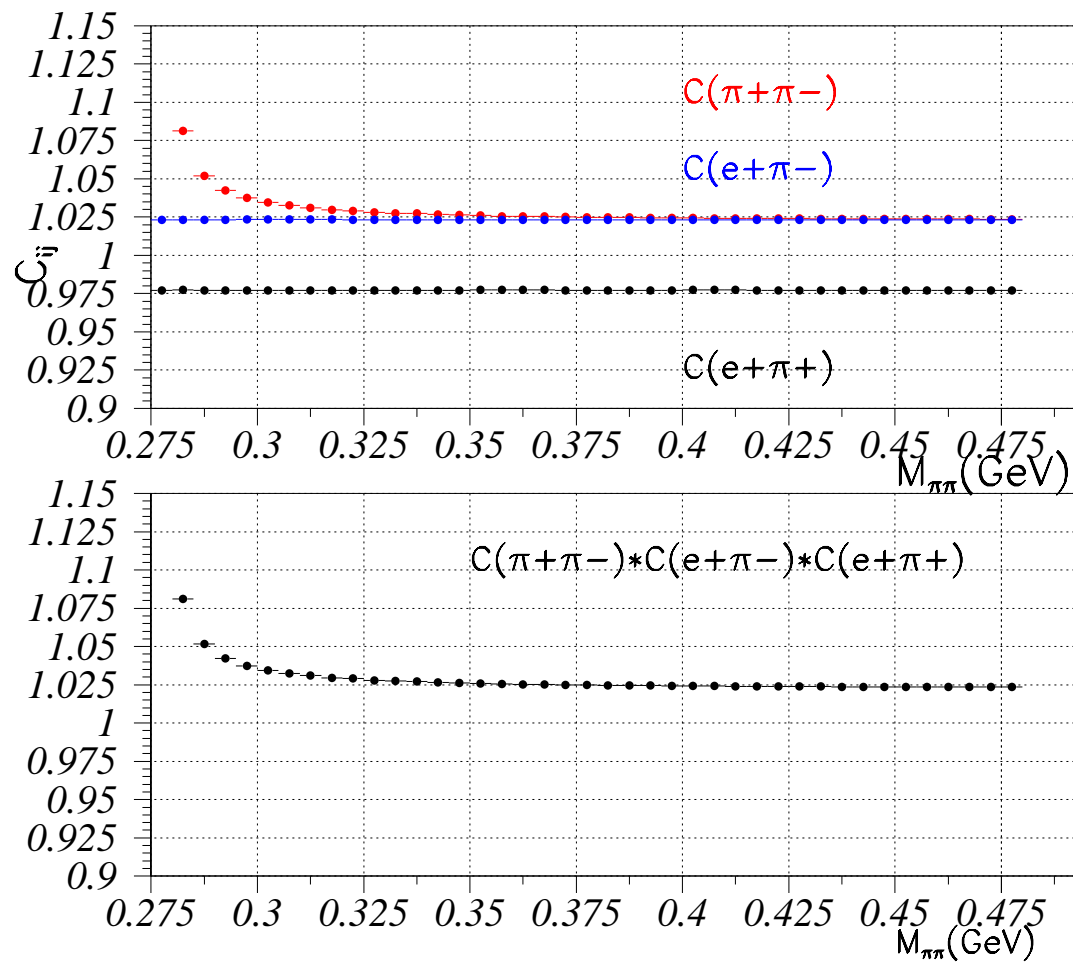
Coulomb correction



Coulomb correction



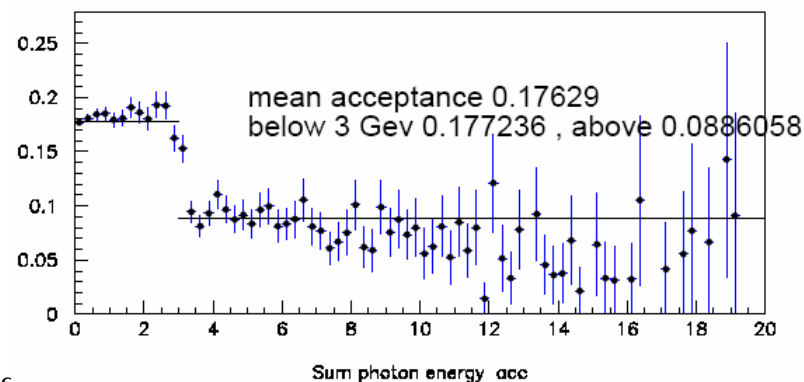
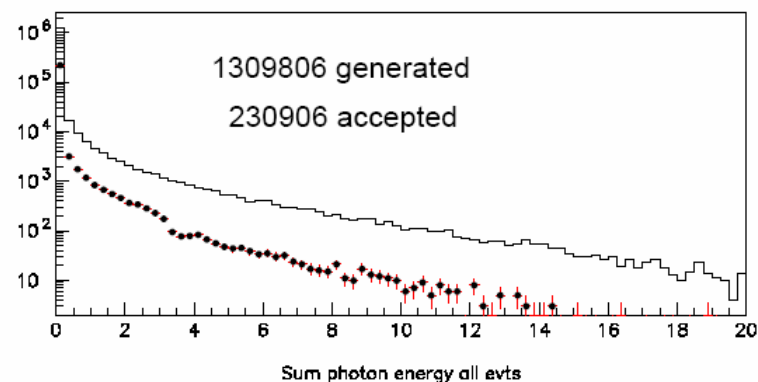
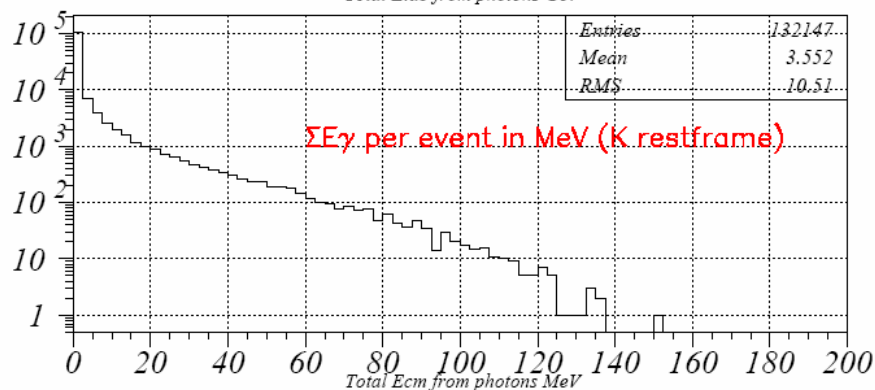
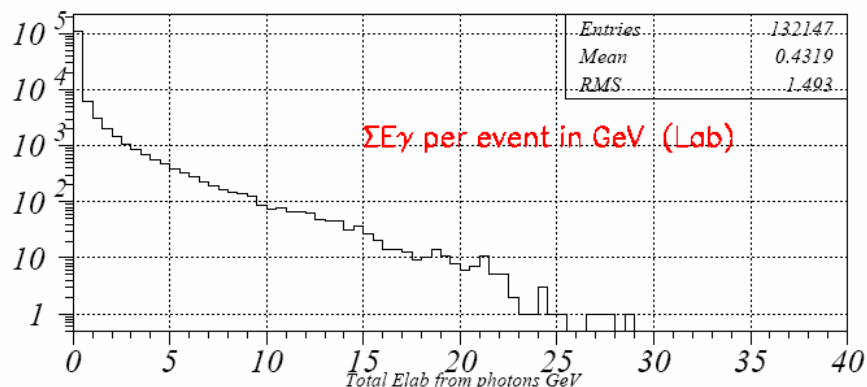
## Coulomb correction

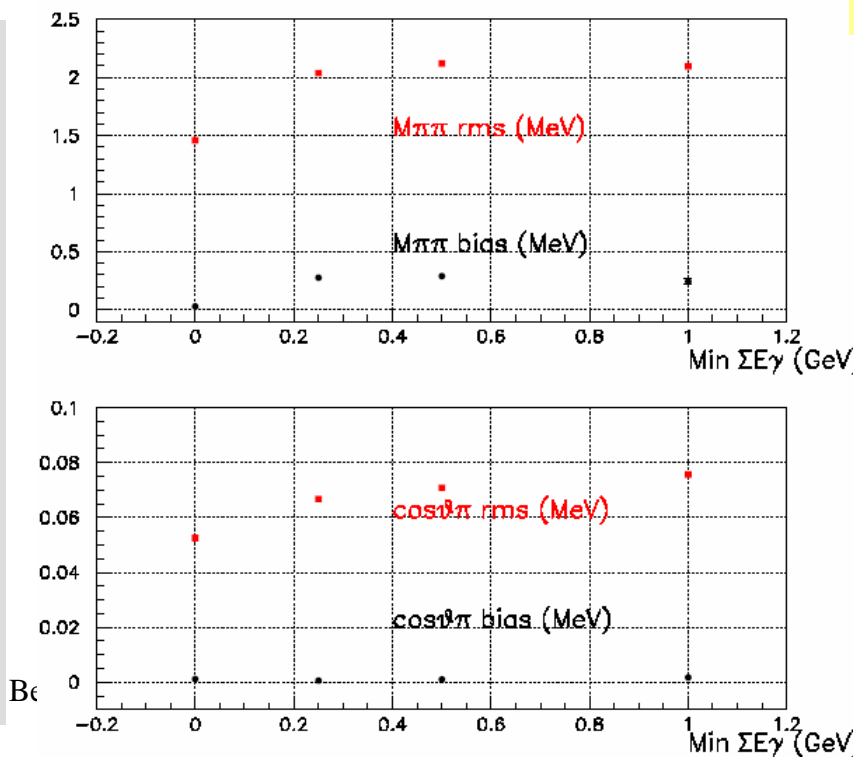
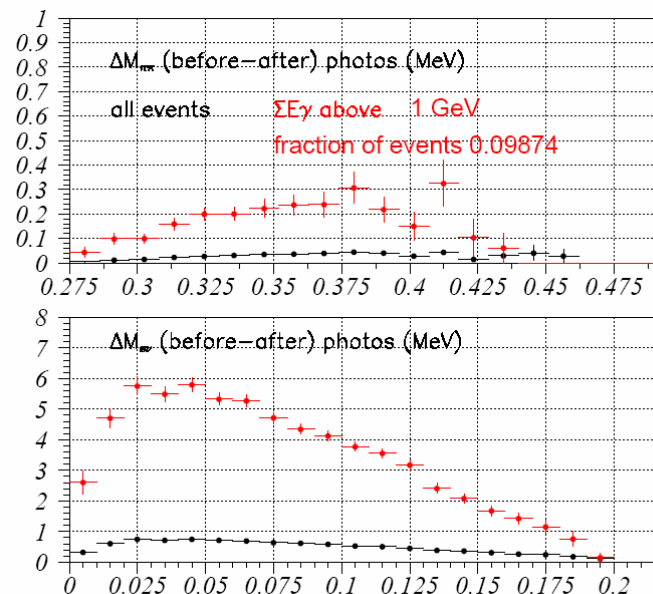
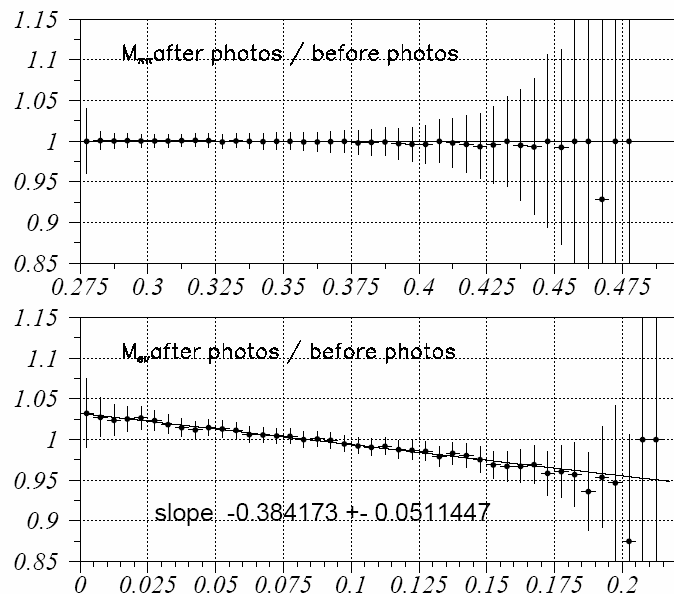


# Radiative corrections

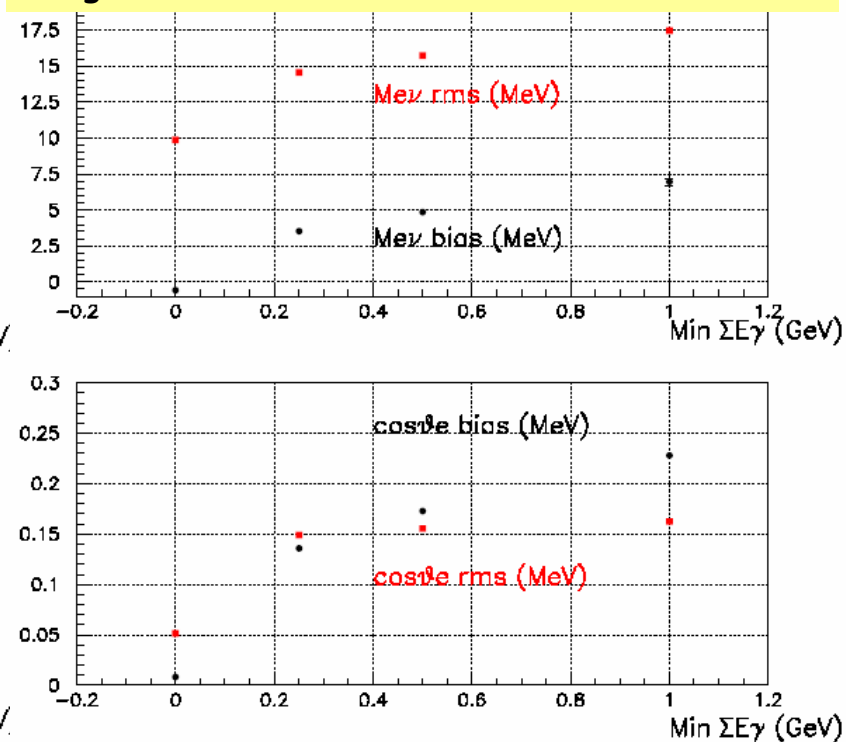
Simulation using PHOTOS version 2.15 from Z. Was et al.

At high  $M_{\pi\pi}$  mass, there is room for photon emission ( and thus at low Mev mass)  
 ~26% of events have "some" radiated photon energy ( $>0$  GeV) but less than  
 10% have more than 1 GeV radiated. Above 3GeV radiated energy, the  
 acceptance is even lower (cut at 3GeV non associated energy)



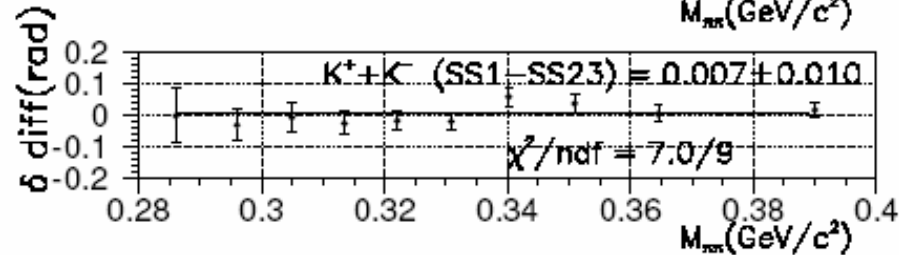
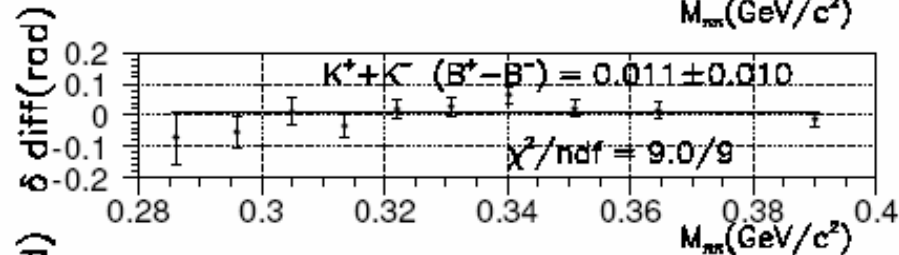
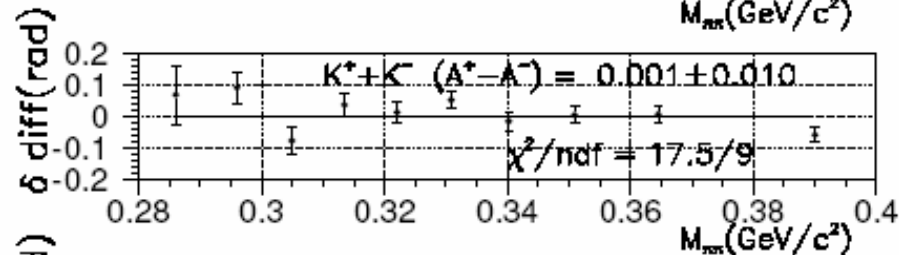
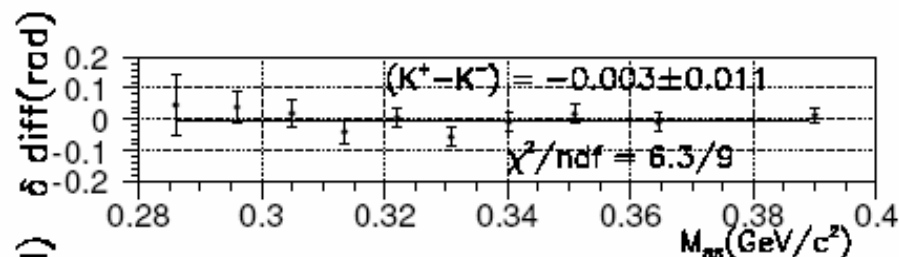
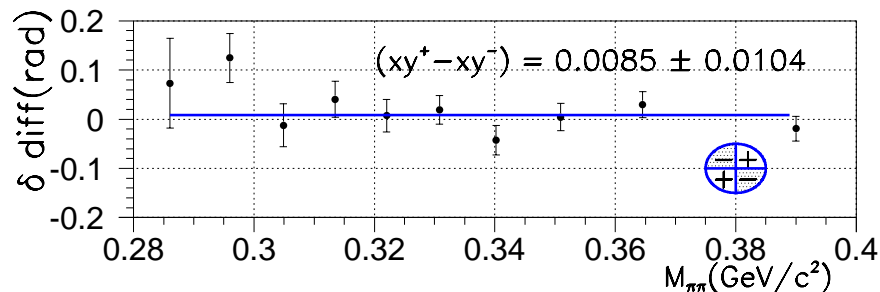
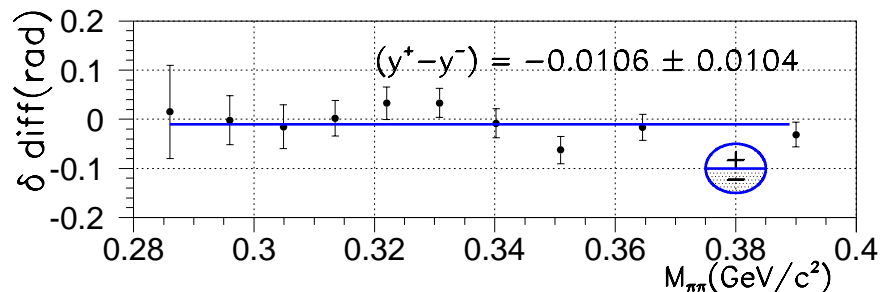
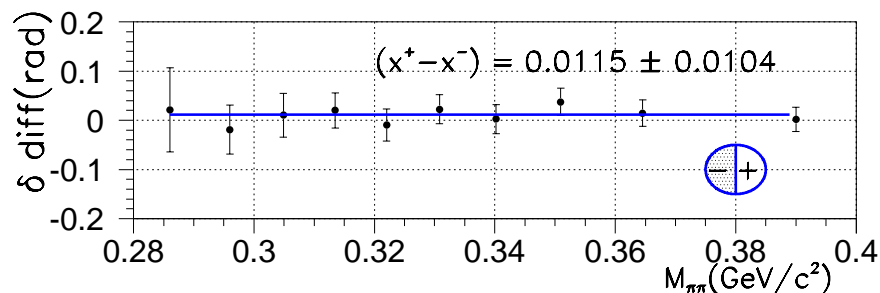


### Largest effect on $M_{\pi\pi}$ and $\cos\theta_{\pi\pi}$ variables



# Stability checks = acceptance control quality

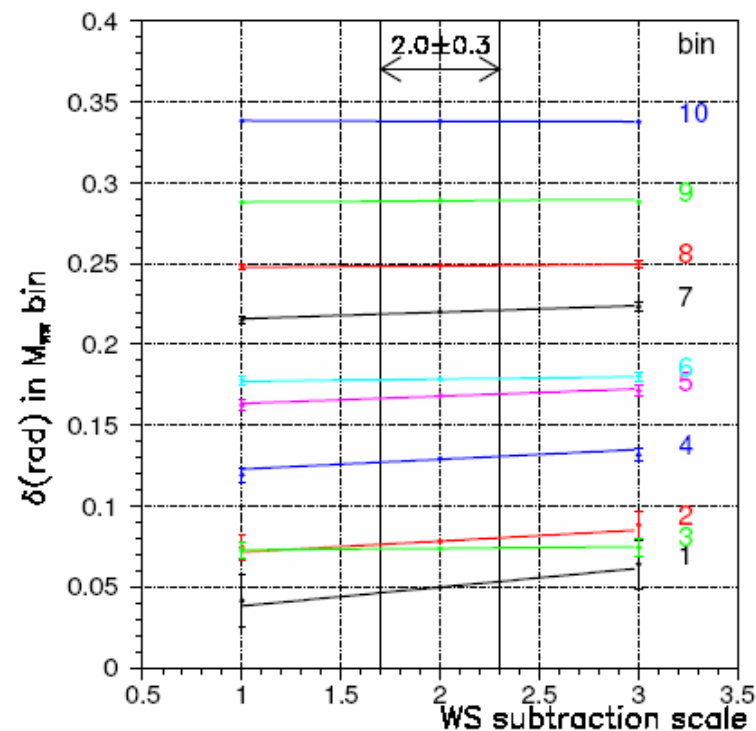
Electron impact in LKr calo, Kaon charge, Achromat and Magnet polarity, time ...



# Background level control (1)

## Method:

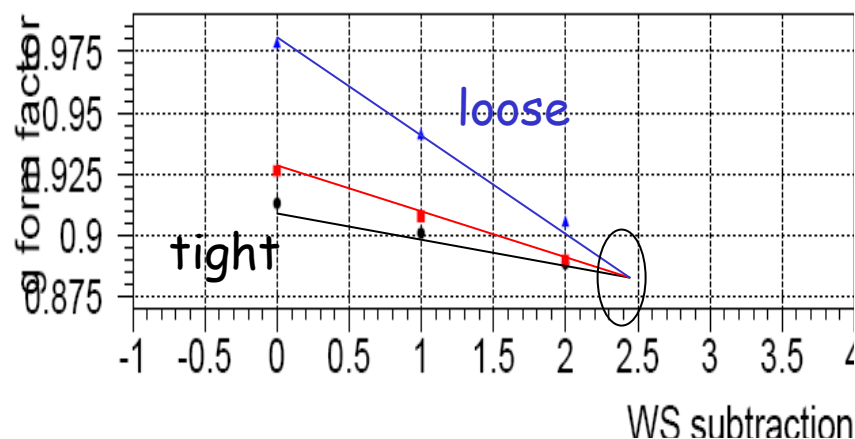
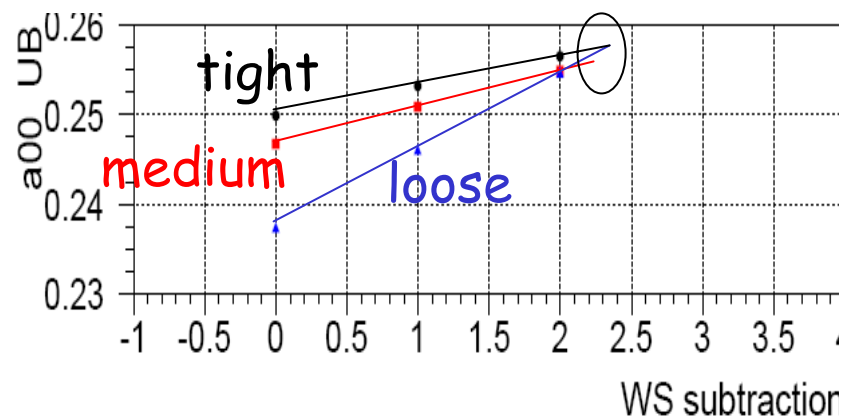
- subtract  $1*WS, 2*WS, 3*WS$
- Measure slope  $D\delta/D_{bkg}$  for each  $\delta$  point



Quote  $0.3*D\delta/D_{bkg}$  since we control the background subtraction as  $(2. \pm 0.3)*WS$

Slopes are all positive, **bin to bin correlated**

- Repeat for 3 ellipse cuts : the FF vary with the level of bkg subtracted but with different slopes
- The 3 lines **focus** to the same FF value when the **true level** is reached =  $\sim 2.3 \times$  Wrong Sign events
- This factor 2.3 confirmed by summing all background processes contributing to signal with corresponding acceptance and branching fractions.

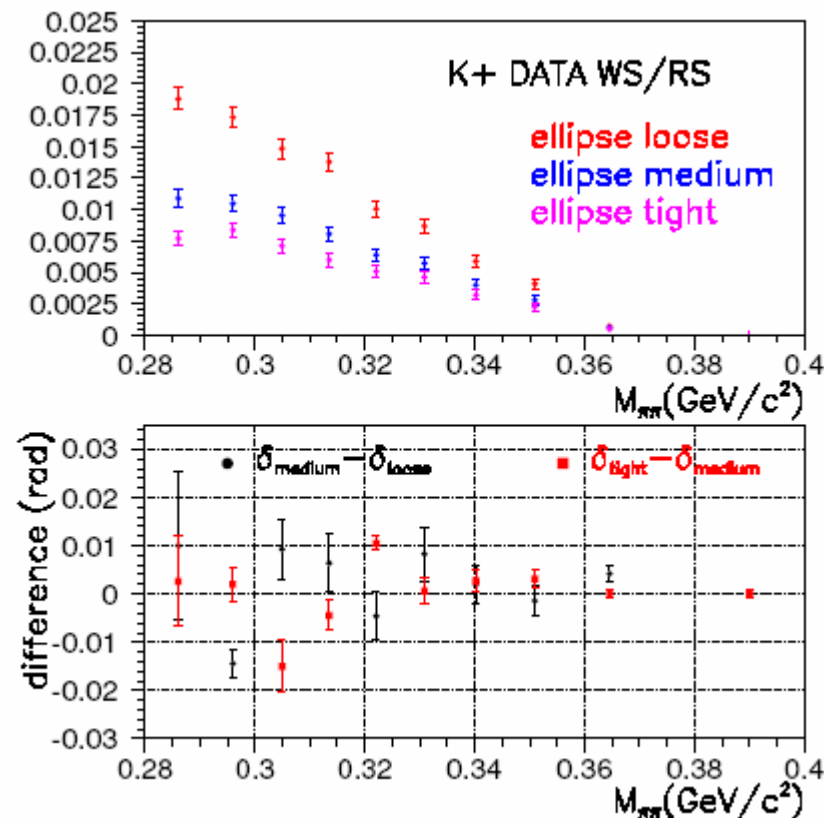




**Method:**

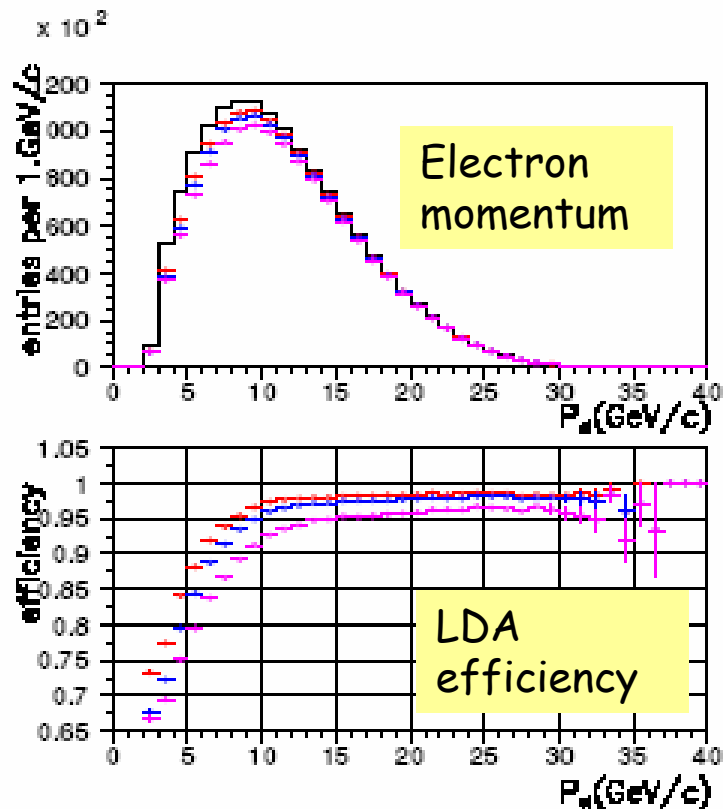
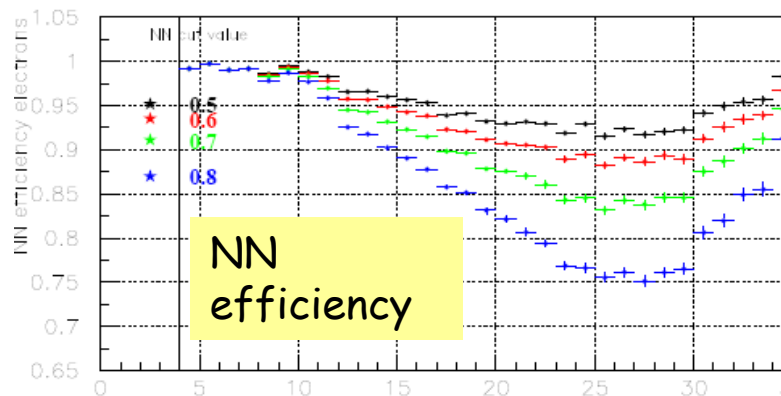
- Vary the ellipse cut in the plane  $[M_{3\pi}-MK, pt]$  from loose to medium to tight
- Background shape distorted ( not scaled)
- Quote  $0.5*(D\delta_1-D\delta_2)$  as variations are similar and remove both  $\sim 2\%$  events

No bin to bin correlation



**Method:**

- Vary the LDA cut = (0.85, 0.90, 0.95) for Data and MC (applied to MC as a parametrized efficiency  $f(P_{\text{el}})$ ),
- + compare NN (0.80) and LDA(0.90) results
- Quote weighted rms of the three numbers as variations are similar and bin to bin uncorrelated

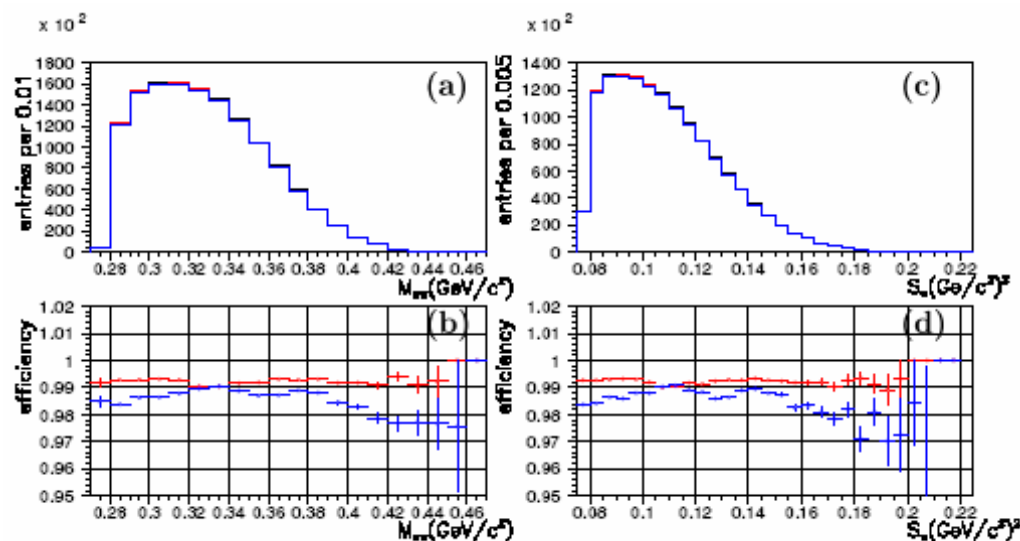


## 2 Methods:

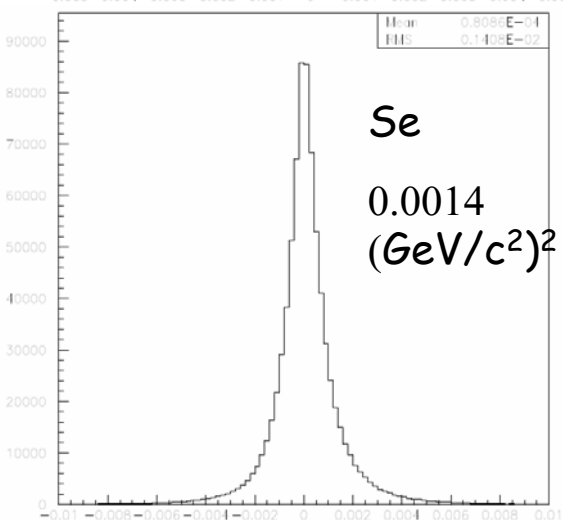
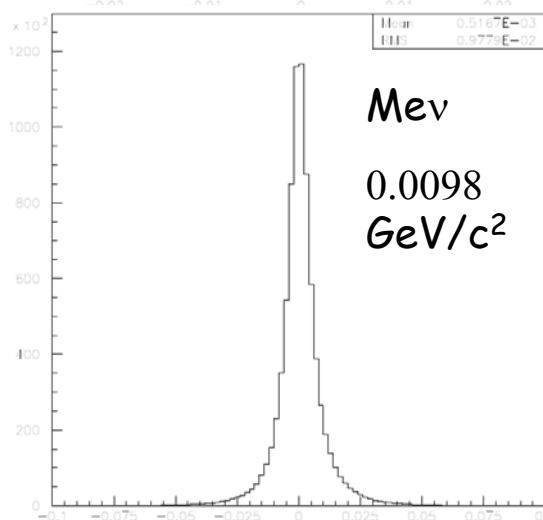
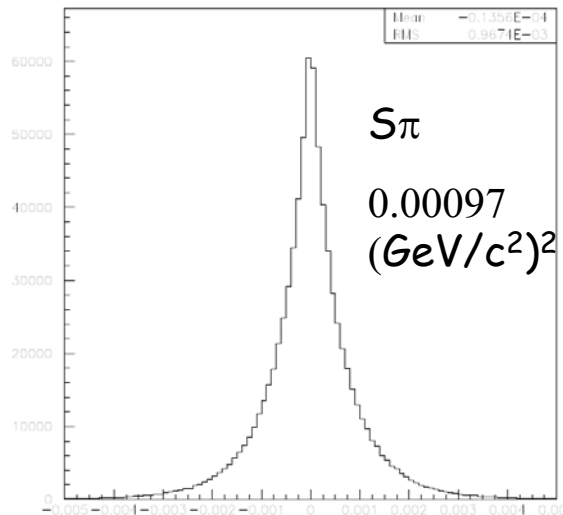
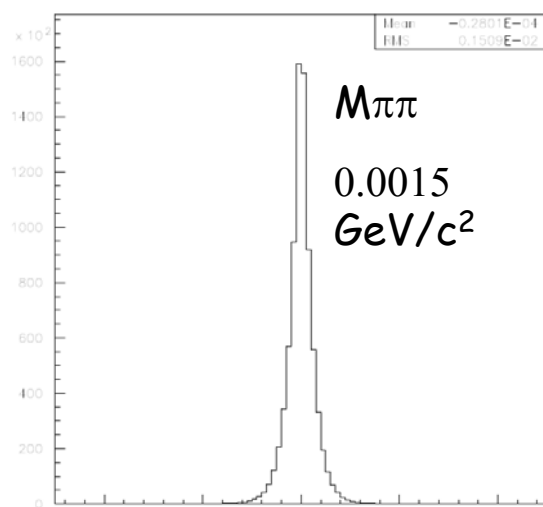
- evaluation from Minimum Bias triggers in 2003:  
 $\text{Efficiency} = (99.3 \pm 0.1)\%$ , available as a matrix in the 5-dimension space of the C.M. variables.
- evaluation from  $\pi\pi^0$  decays treated as  $\text{Ke}4$  ( $S_\pi$  up to 0.225)  
 $\text{Efficiency} = (98.15 \pm 0.06)\%$ , available as function of  $S_\pi$

Difference within 1% for significant acceptance regions

Effect on data is similar when efficiency applied to MC,  $\rightarrow$  average values, bin to bin uncorrelated



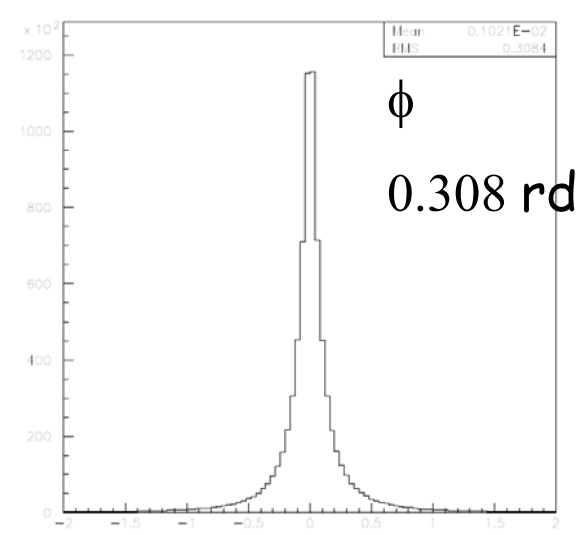
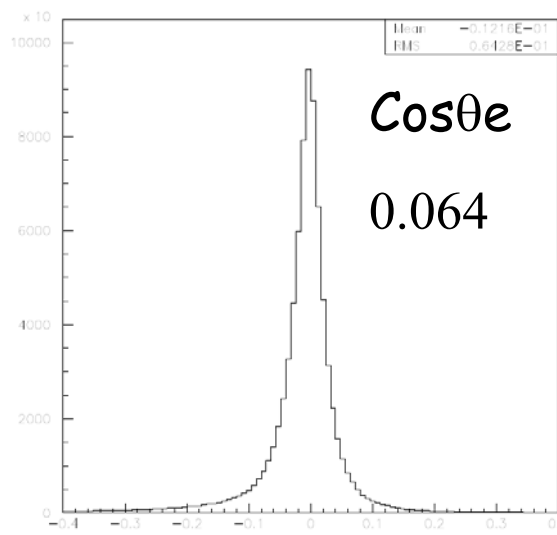
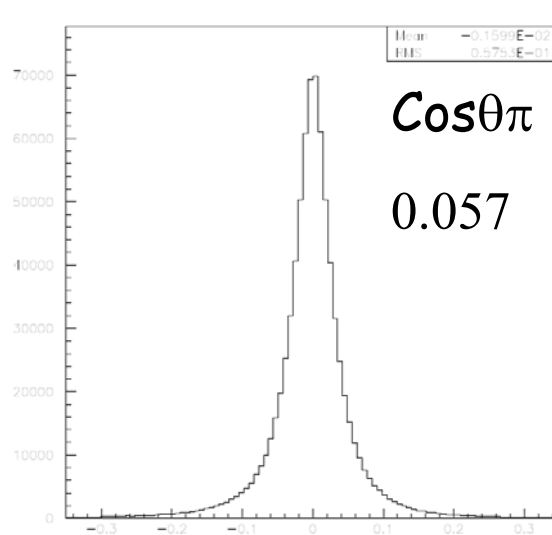
## Resolution for C.M. variables : masses



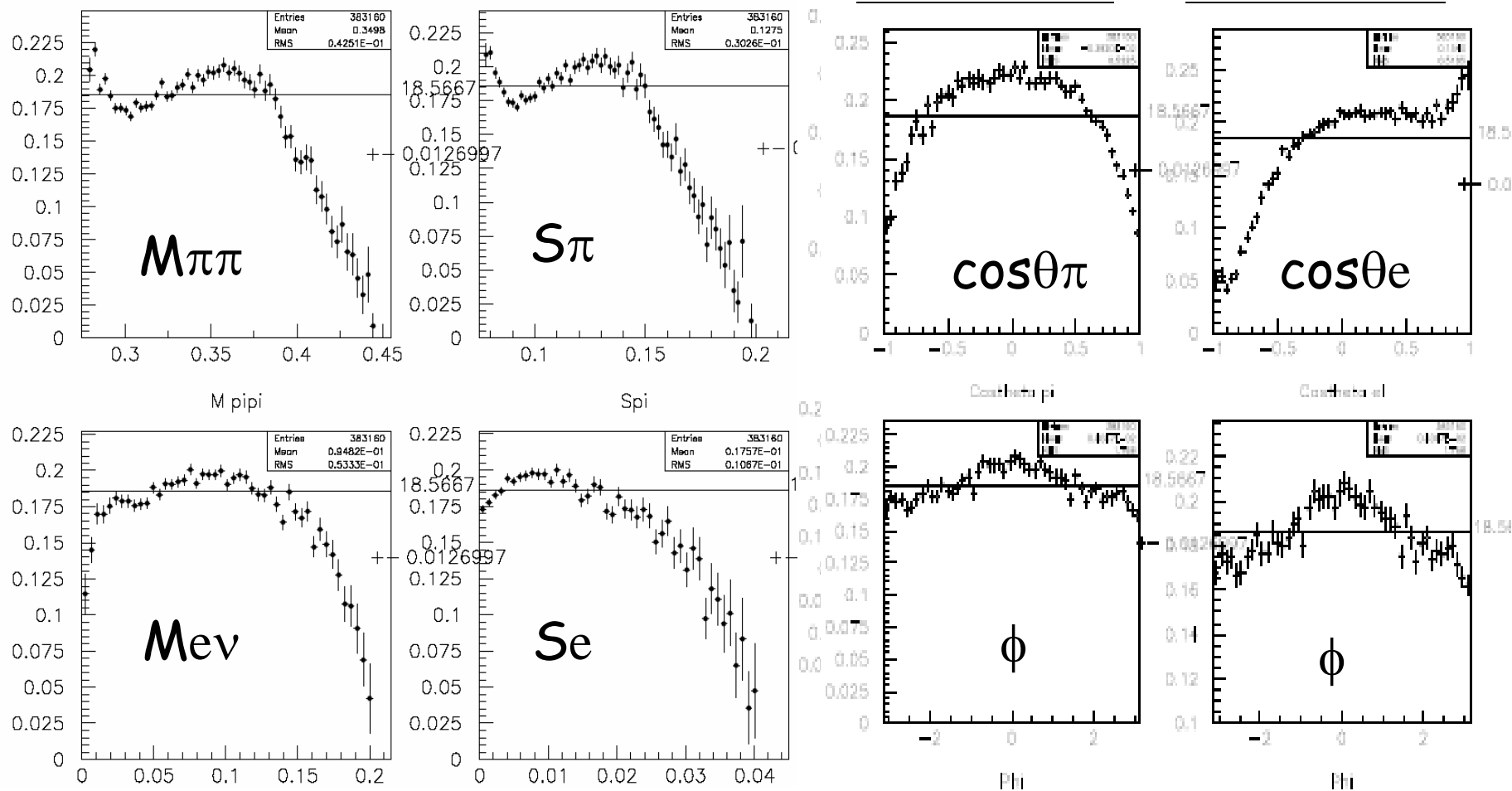
BNL for comparison :

 $S_{\pi}$  0.00133  $(\text{GeV}/c^2)^2$  $S_e$  0.00361  $(\text{GeV}/c^2)^2$  $\theta_{\pi}$  0.147 (rad) $\theta_e$  0.111 (rad) $\phi$  0.404 (rad)

## Resolution for C.M. variables : rms (angles)



Typically  $18.57 \pm 0.01 \%$



The "Dalitz" plot ( $M_{\pi\pi}, M_{e\nu}$ ) bins